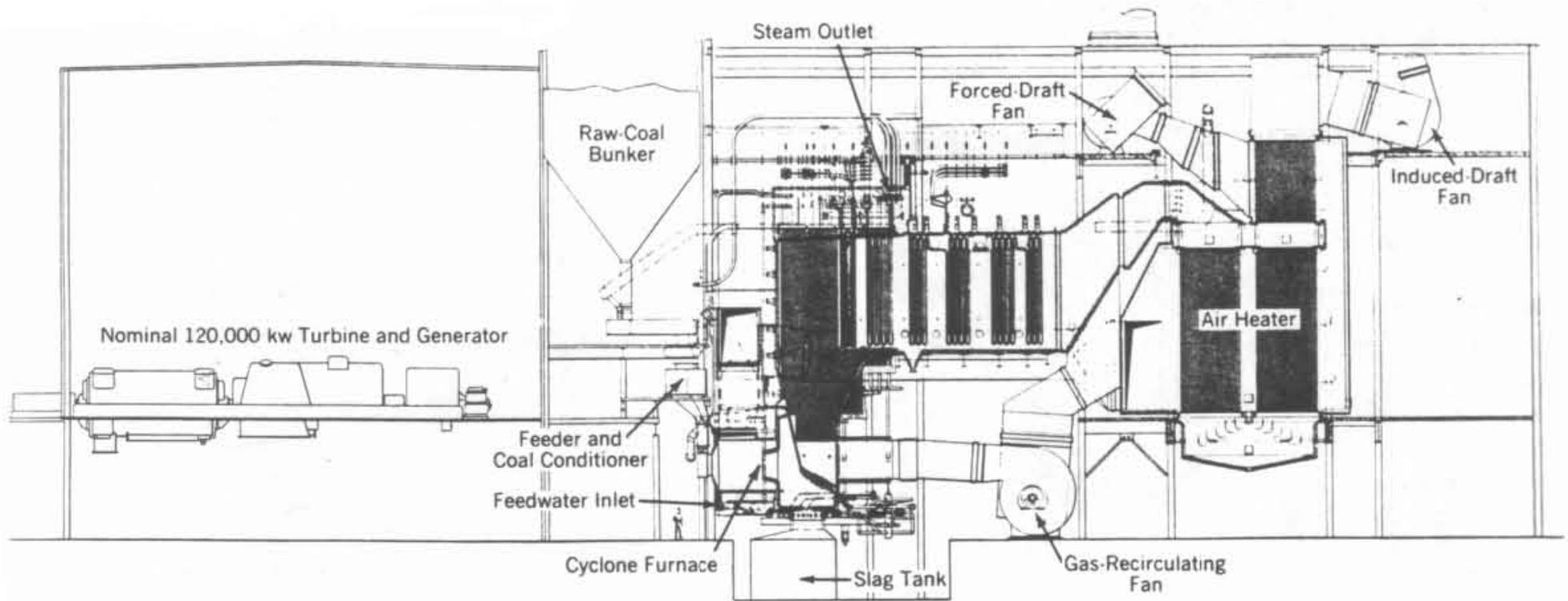


Industrial motivation



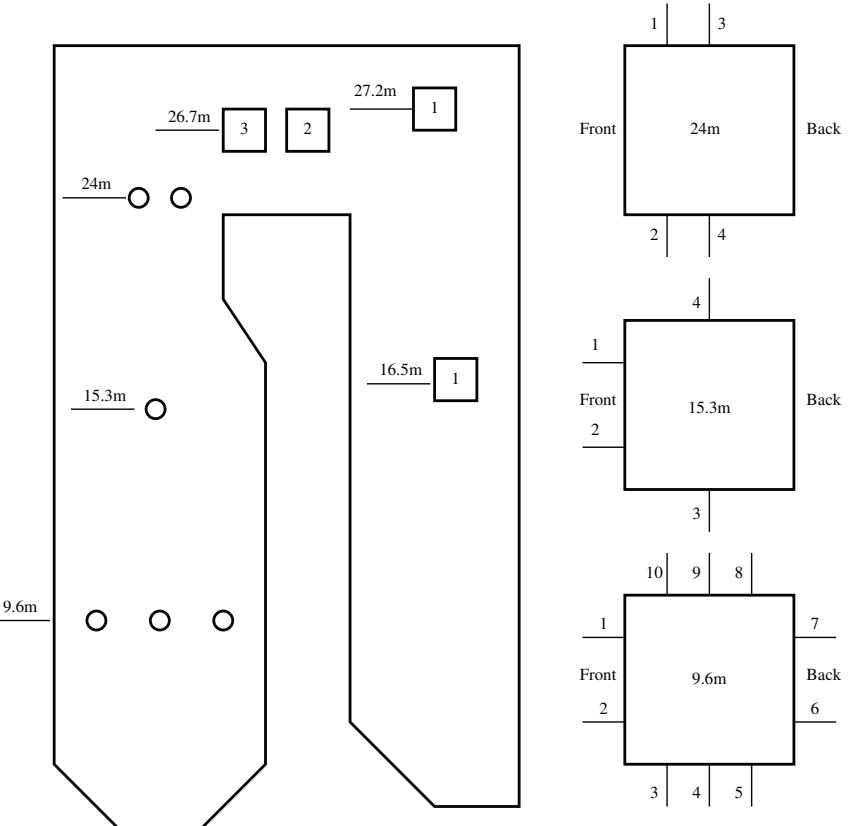
Steam generator in a power plant

S. C. Schultz. Steam, Its Generation and Use, 40th ed. Babcock & Wilcox Company, 1992

Industrial motivation

Important processes

- gas flow in the large scale burners
- combustion processes described by physical principles (burnout measured data)
- NOx chemistry
- energy release and transfer to water piping
- co-firing - simultaneous combustion of biofuel

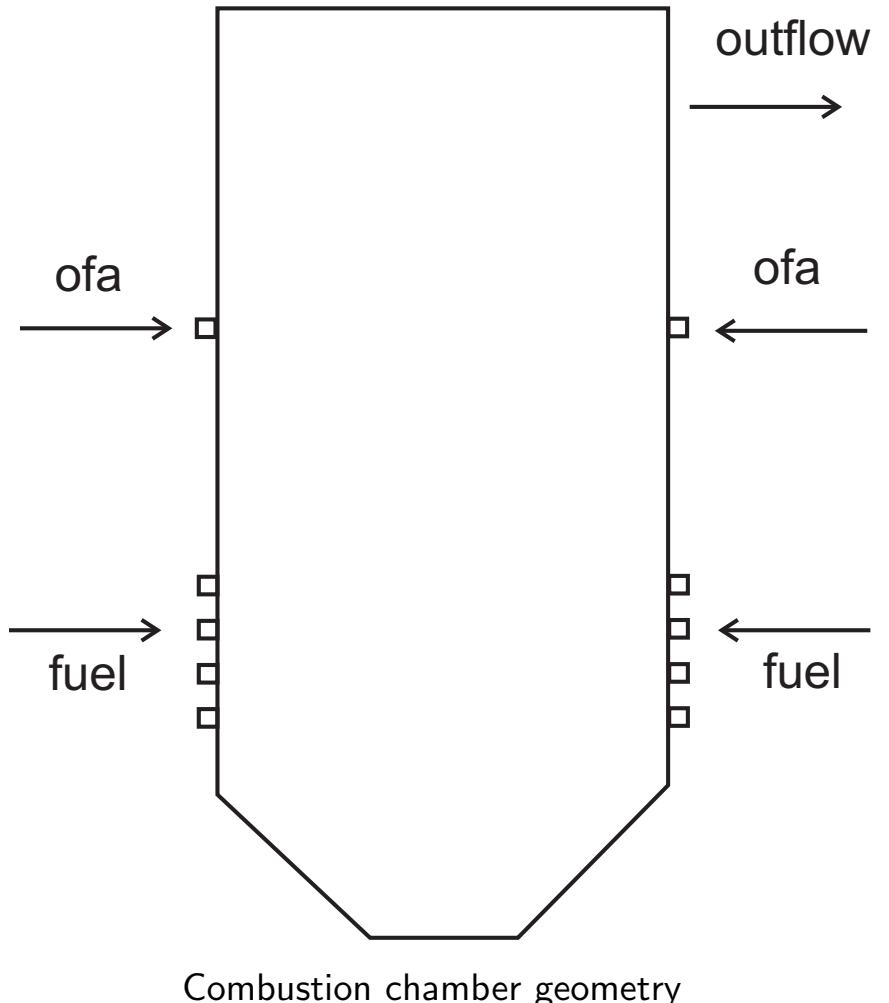


Measurement points in the burner

Geometry

Geometry

- inlet - burners - mixing
 - powdered coal
 - air
 - biofuel
- outlet - artificially underpressurized flue gas outflow
- walls transferring heat outwards
- over-fire air inlet (OFA)



Mass conservation

Total-mass balance and chemical components balance laws

$$\begin{aligned}\frac{\partial \rho}{\partial t} + \frac{\partial(\rho v_i)}{\partial x_i} &= 0 \\ \frac{\partial}{\partial t}(\rho Y_*) + \frac{\partial}{\partial x_i}(\rho Y_* v_i) &= \frac{\partial}{\partial x_i} \left(-\frac{\mu_T}{Sc_t} \frac{\partial Y_*}{\partial x_i} \right) + \omega_*\end{aligned}$$

where * substitutes O₂, N₂, NO, HCN, NH₃, H₂O and CO₂

Char, volatiles and coal particle balance laws

$$\begin{aligned}\frac{\partial \rho_{char}}{\partial t} + \frac{\partial(\rho_{char} v_i)}{\partial x_i} &= R_{char} \\ \frac{\partial \rho_{vol}}{\partial t} + \frac{\partial(\rho_{vol} v_i)}{\partial x_i} &= R_{vol} \\ \frac{\partial n}{\partial t} + \frac{\partial(n v_i)}{\partial x_i} &= 0\end{aligned}$$

Flow and heat transfer

Momentum and energy balance laws

$$\begin{aligned}\frac{\partial}{\partial t}(\rho v_i) + \frac{\partial}{\partial x_i}(p + \rho v_i^2) &= \frac{\partial}{\partial x_j} \left(\mu \frac{\partial v_i}{\partial x_j} \right) + \frac{1}{3} \frac{\partial}{\partial x_j} \left(\mu \frac{\partial v_j}{\partial x_i} \right) - \frac{2}{3} \frac{\partial}{\partial x_i}(\rho k) + \rho g_i \\ c_p \left[\frac{\partial}{\partial t}(\rho T) + \frac{\partial}{\partial x_i}(\rho T v_i) \right] &= -R_{\text{char}} h_{\text{char}} - R_{\text{vol}} h_{\text{vol}} - \nabla(\mathbf{q}_c + \mathbf{q}_r) + \frac{\partial}{\partial x_j} \left[\left(\mu_L + \frac{\mu_T}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right]\end{aligned}$$

$k - \varepsilon$ model for turbulence

$$\begin{aligned}\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k v_i) &= \frac{\partial}{\partial x_j} \left[\left(\mu_L + \frac{\mu_T}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + G_k - G_b - Y_m - \rho \varepsilon \\ \frac{\partial}{\partial t}(\rho \varepsilon) + \frac{\partial}{\partial x_i}(\rho \varepsilon v_i) &= \frac{\partial}{\partial x_j} \left[\left(\mu_L + \frac{\mu_T}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial x_j} \right] + C_{1\varepsilon} \frac{\varepsilon}{k} (G_k + C_{3\varepsilon} G_b) - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k}\end{aligned}$$

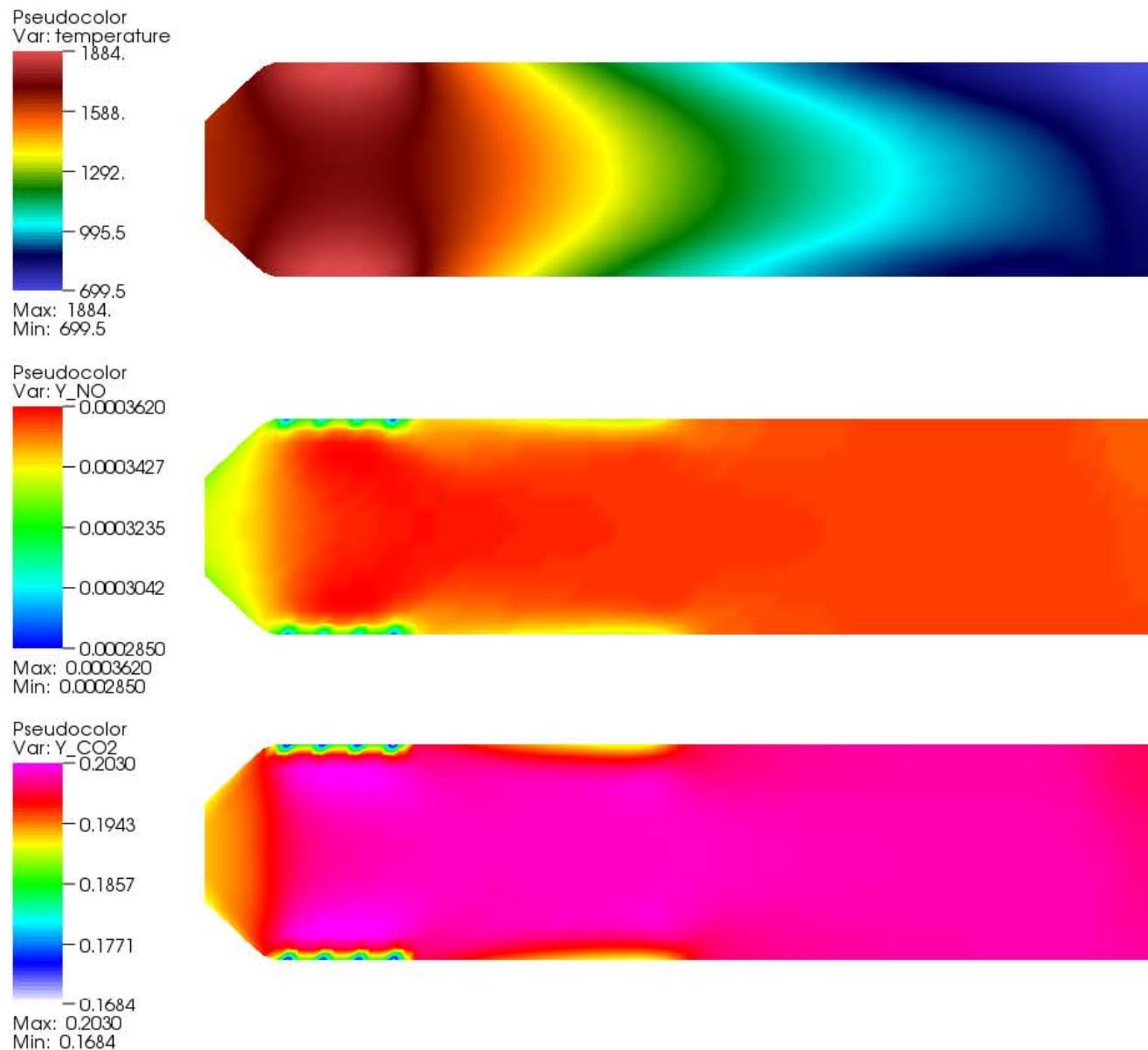
$$\begin{aligned}p &= \frac{\rho RT}{\bar{M}}, \quad \mu_T = \rho C_\mu \frac{k^2}{\varepsilon}, \quad \mu = \mu_L + \mu_T, \quad h_{\text{char}} + h_{\text{vol}} = LHV \\ G_k &= \left(\frac{\partial v_1}{\partial x_2} + \frac{\partial v_2}{\partial x_1} \right)^2 + \frac{\partial v_1}{\partial x_1} \left[\frac{4}{3} \mu \frac{\partial v_1}{\partial x_1} - \frac{2}{3} \left(\rho k + \mu \frac{\partial v_2}{\partial x_2} \right) \right] + \frac{\partial v_2}{\partial x_2} \left[\frac{4}{3} \mu \frac{\partial v_2}{\partial x_2} - \frac{2}{3} \left(\rho k + \mu \frac{\partial v_1}{\partial x_1} \right) \right] \\ G_b &= -g_i \frac{\mu}{\rho P r_t} \frac{\partial \rho}{\partial x_i}, \quad C_{3\varepsilon} = \tanh \left| \frac{v_2}{v_1} \right|, \quad Y_m = 2\rho \varepsilon M_t^2, \quad M_t = \sqrt{\frac{k}{a^2}}, \quad a = \sqrt{\gamma RT}\end{aligned}$$

Simulation results

Case	Air distribution %				Fuel distribution %				Excess air coefficient				NO ppm	CO ₂	O ₂
	B ₁	B ₂	B ₃	B ₄	B ₁	B ₂	B ₃	B ₄	B ₁	B ₂	B ₃	B ₄			
1	25	25	25	25	25	25	25	25	1.3	1.3	1.3	1.3	357	20%	1.9%
2	50	20	20	10	25	25	25	25	2.6	1.04	1.04	0.52	177	20%	1.9%
3	10	20	20	50	25	25	25	25	0.52	1.04	1.04	2.6	134	20%	2%
4	25	25	25	25	50	20	20	10	0.65	1.63	1.63	3.25	182	18%	4.5%

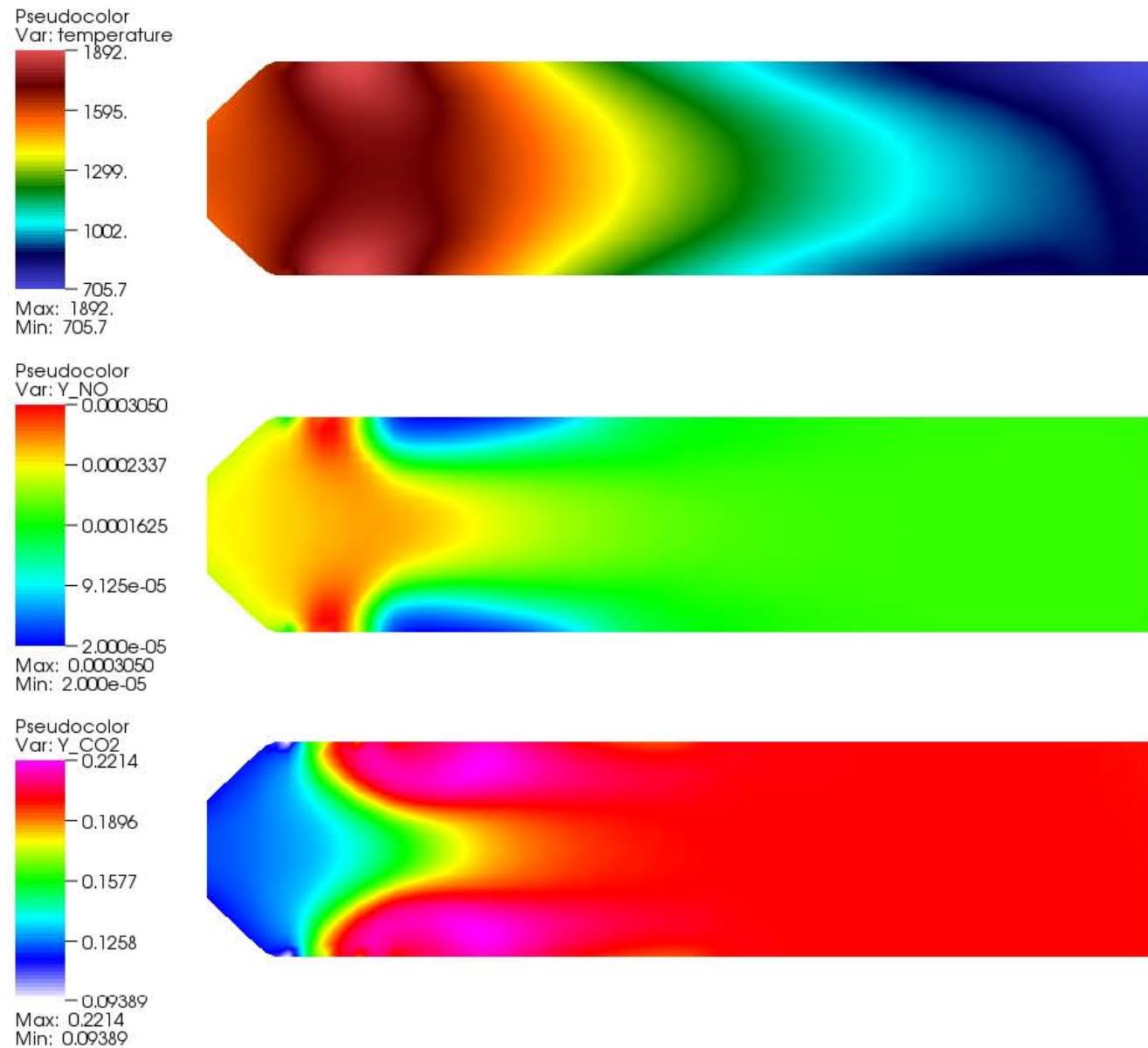
- **Case 1** - uniform air and coal distribution over 4 pairs of burners
- **Case 2** - decreasing air and uniform coal distribution over 4 pairs of burners (with consequent excess or missing air fraction in burners)
- **Case 3** - increasing air and uniform coal distribution over 4 pairs of burners (with consequent excess or missing air fraction in burners)
- **Case 4** - uniform air and decreasing coal distribution over 4 pairs of burners (with consequent excess or missing air fraction in burners)

Simulation results - Case 1



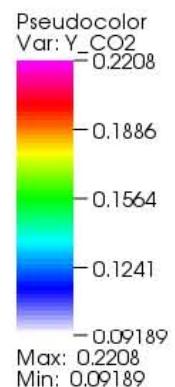
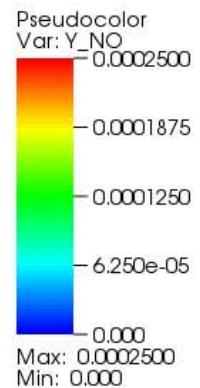
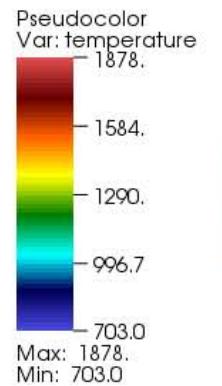
Case 1: Profiles of temperature (top), mass fraction of NO (middle) and mass fraction of CO₂ (bottom)

Simulation results - Case 2



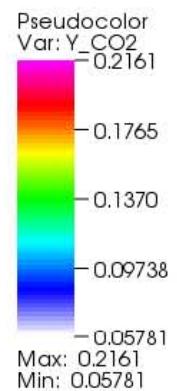
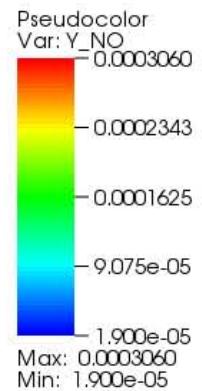
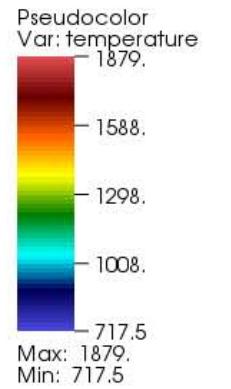
Case 2: Profiles of temperature (top), mass fraction of NO (middle) and mass fraction of CO₂ (bottom)

Simulation results - Case 3



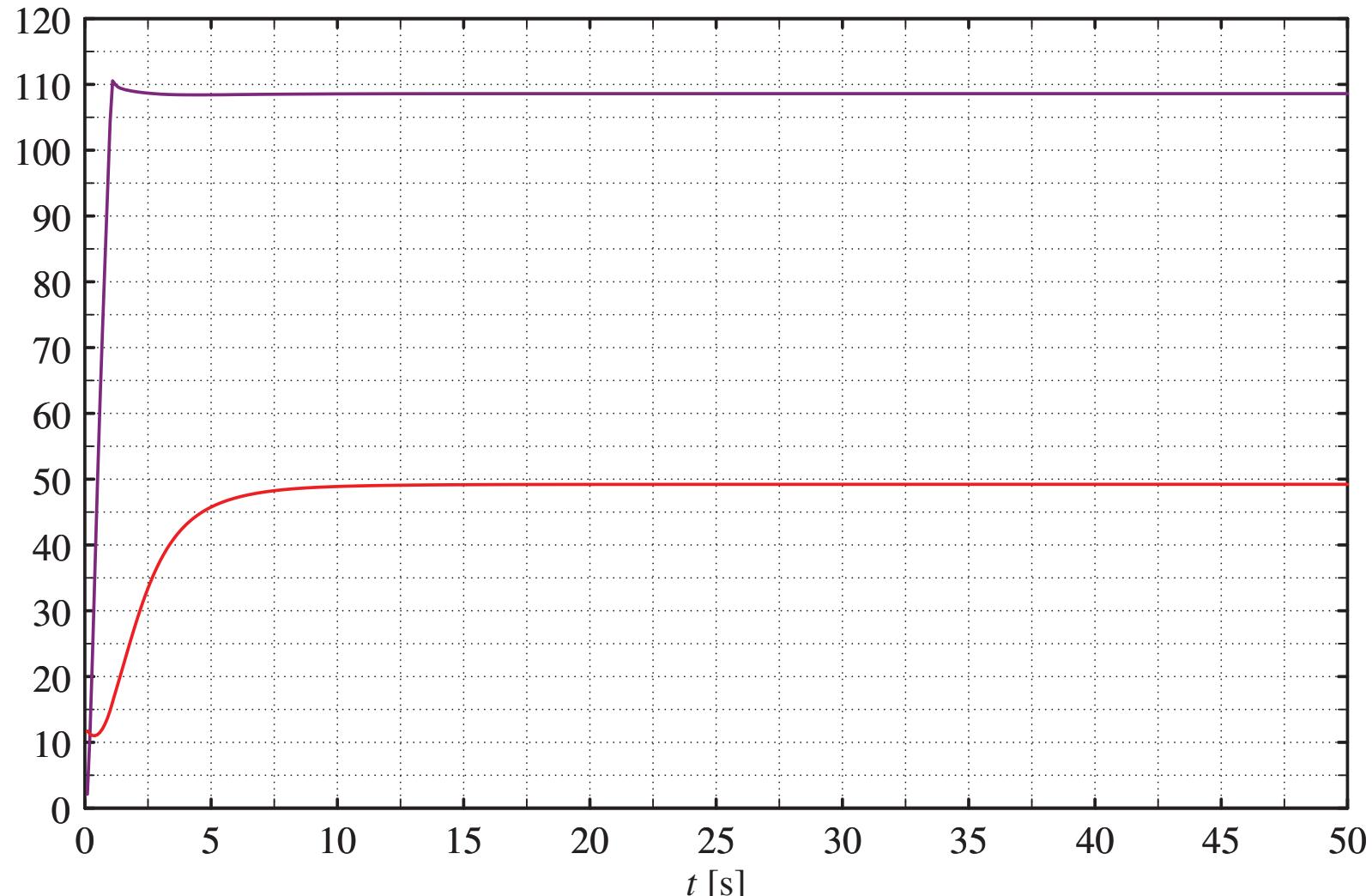
Case 3: Profiles of temperature (top), mass fraction of NO (middle) and mass fraction of CO₂ (bottom)

Simulation results - Case 4



Case 4: Profiles of temperature (top), mass fraction of NO (middle) and mass fraction of CO₂ (bottom)

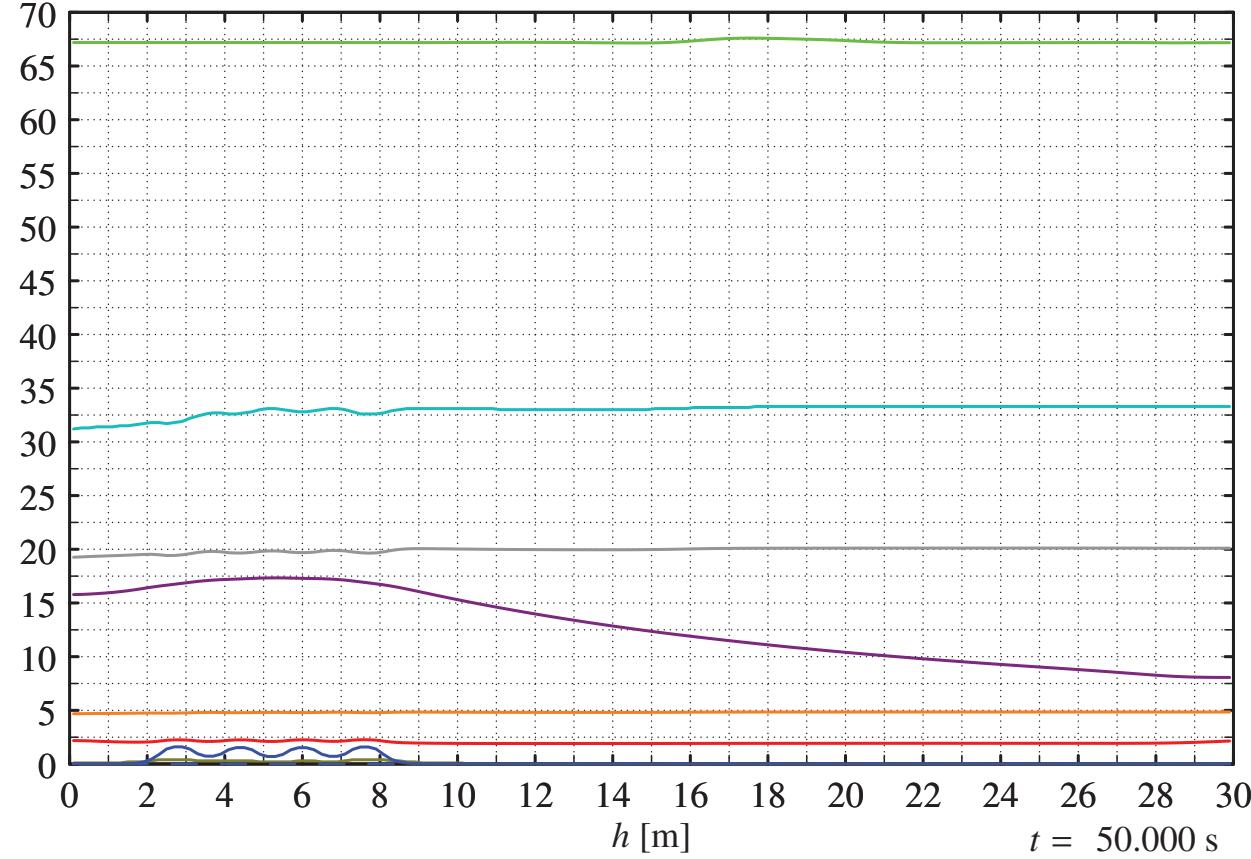
Simulation results - uniform burner composition



— Total heating value [MW] — Heat transfer to walls [MW]

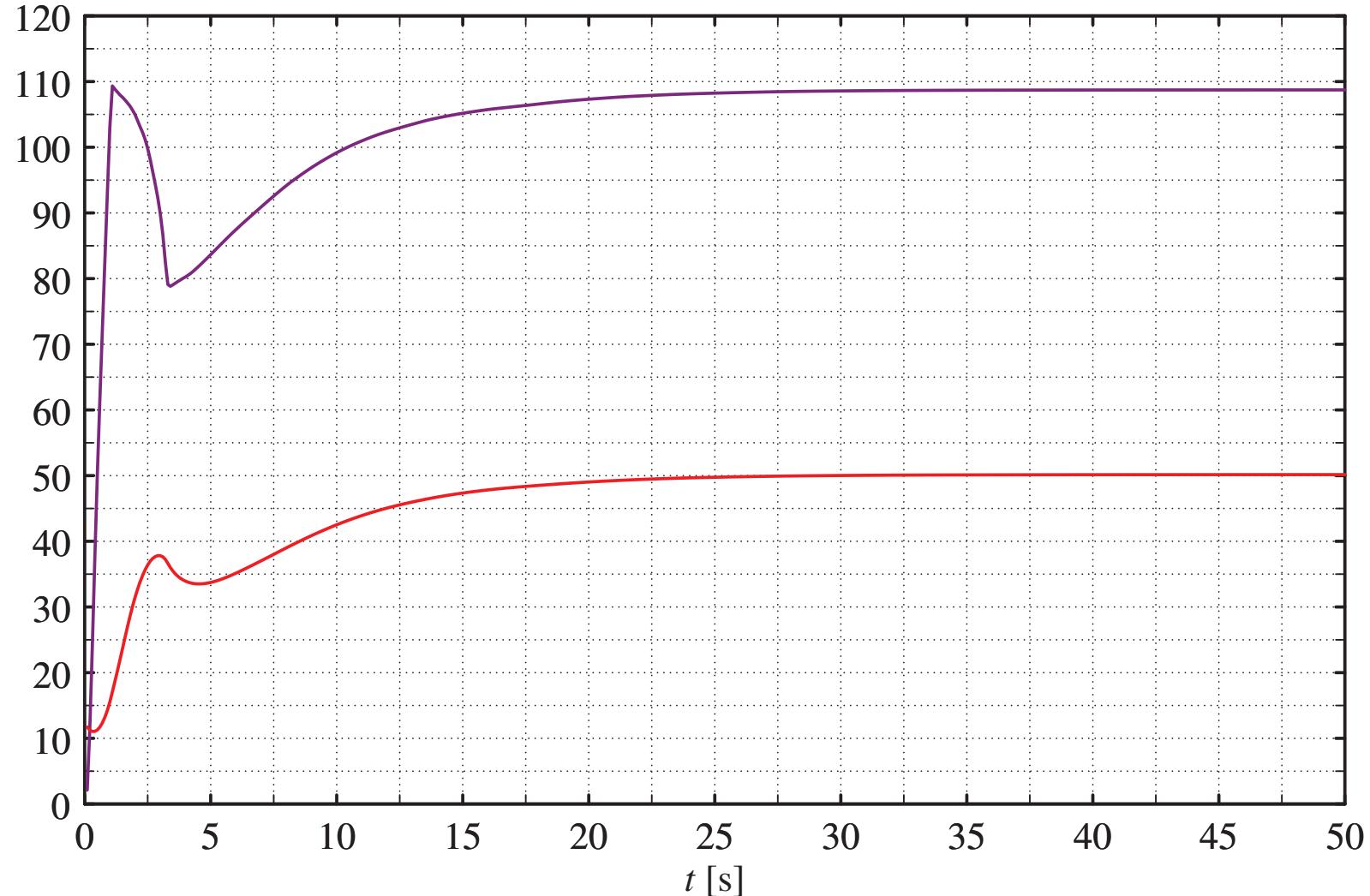
Time evolution of energy release and wall transfer

Simulation results - uniform burner composition



Vertical distribution of key system variables at a given time

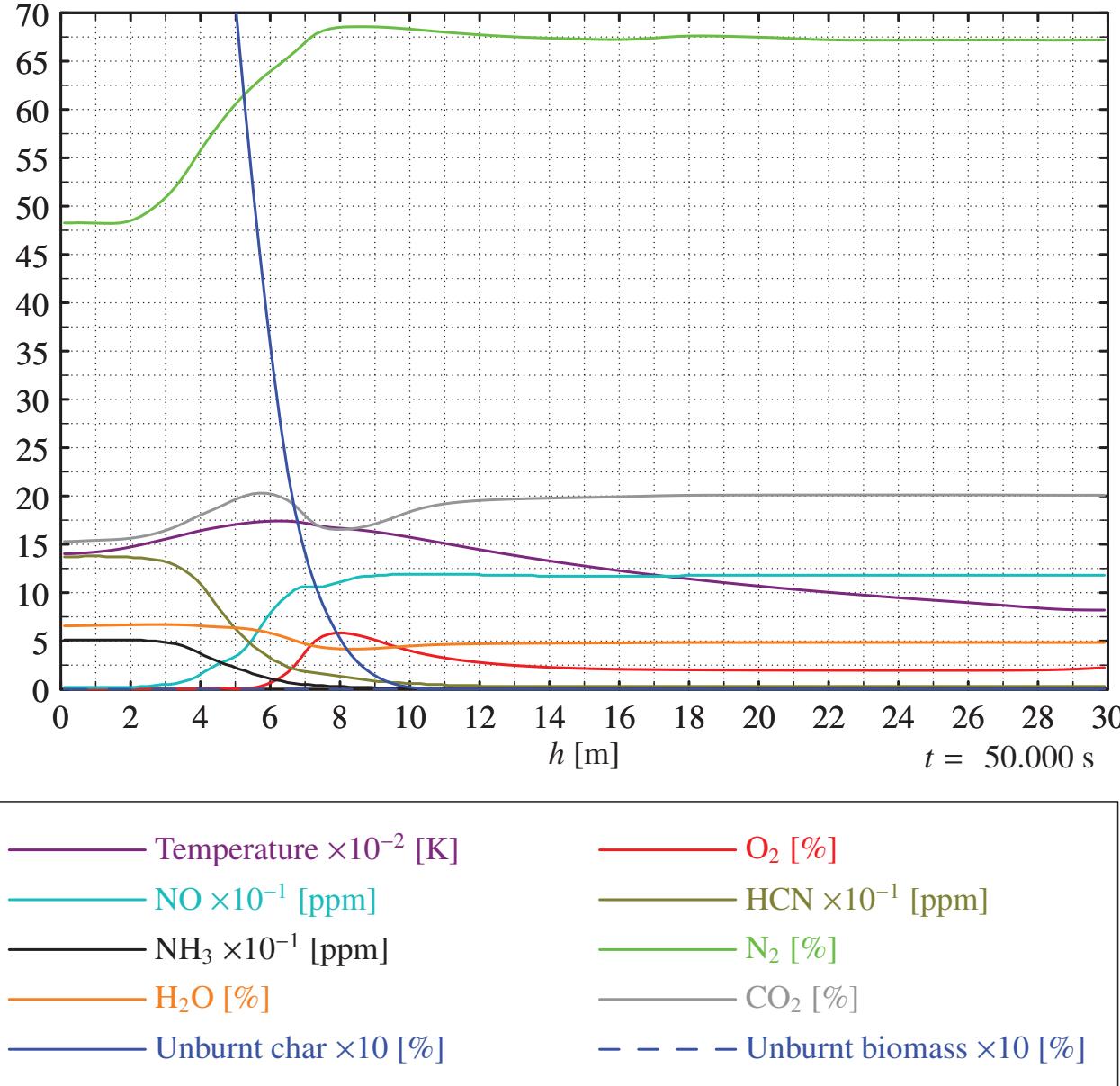
Simulation results - staging 10, 20, 20, 50% air x coal



— Total heating value [MW] — Heat transfer to walls [MW]

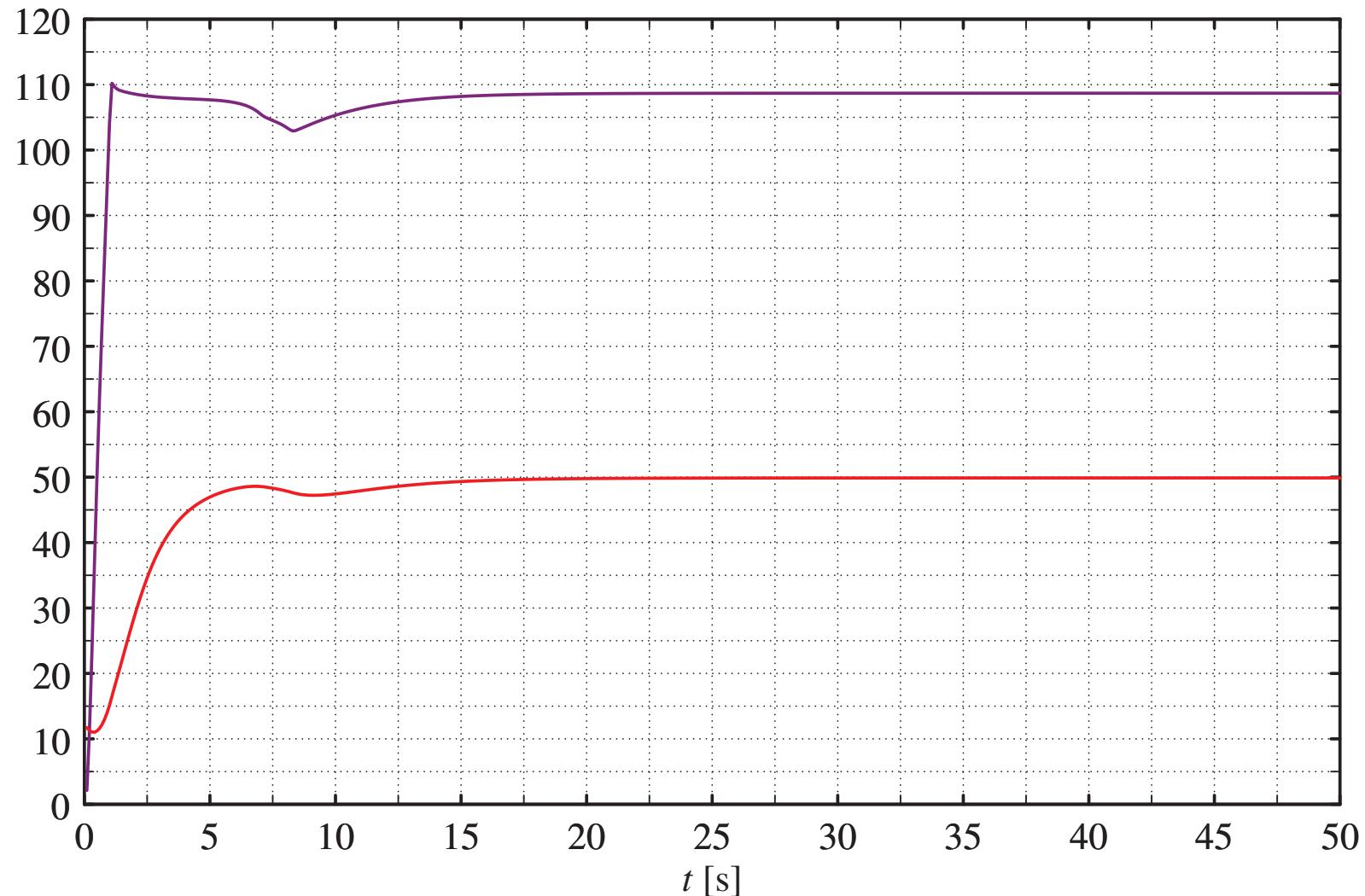
Time evolution of energy release and wall transfer

Simulation results - staging



Vertical distribution of key system variables at a given time

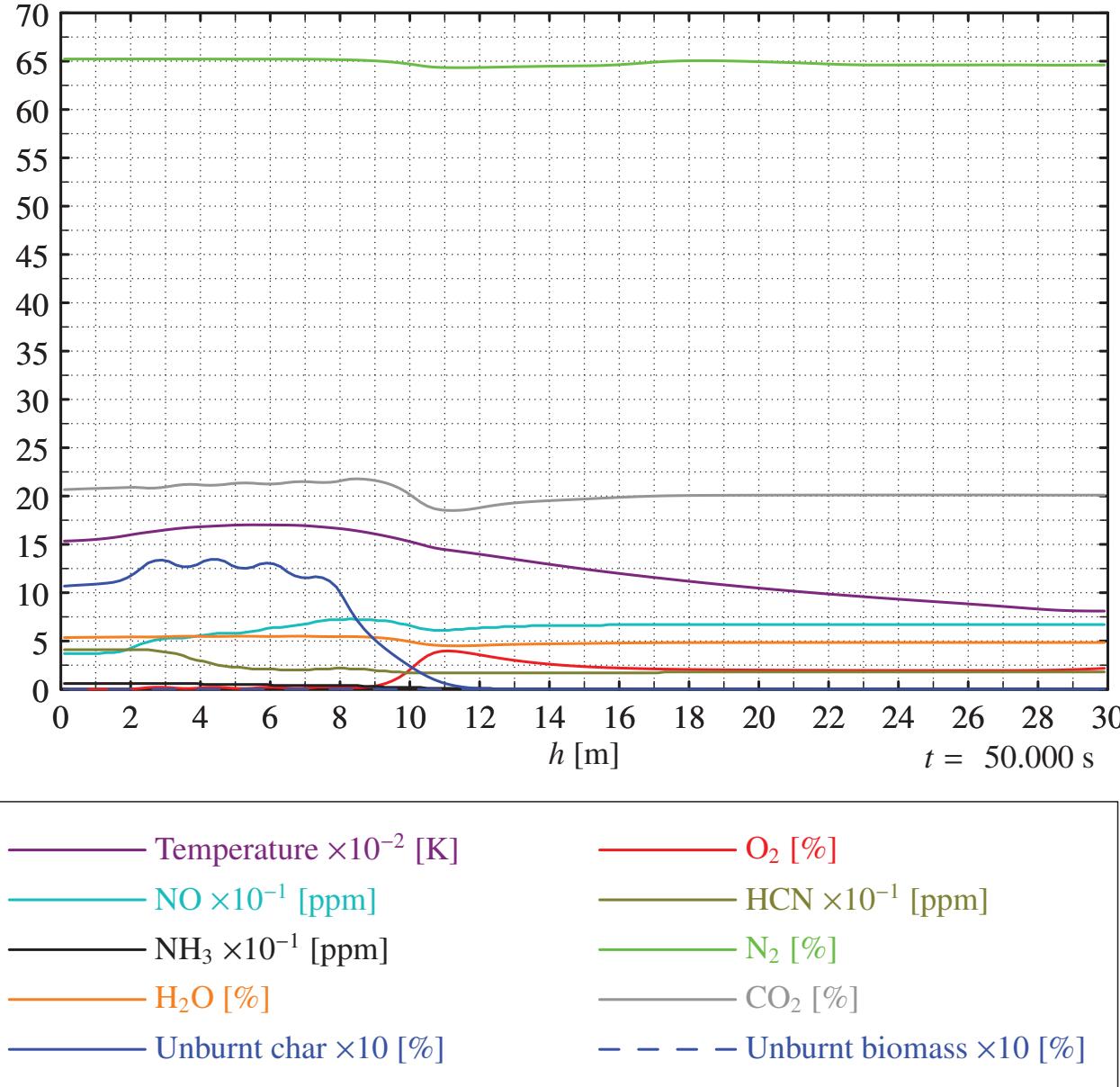
Simulation results - OFA



— Total heating value [MW] — Heat transfer to walls [MW]

Time evolution of energy release and wall transfer

Simulation results - OFA



Vertical distribution of key system variables at a given time